

**CBSE Class 12 physics**  
**Important Questions**  
**Chapter 12**  
**Atoms**

---

**1 Mark Questions**

**1. Name the series of hydrogen spectrum lying in ultraviolet and visible region?**

**Ans.** Lyman series in ultraviolet region and Balmer series in visible region.

---

**2. What is Bohr's quantisation condition for the angular momentum of an electron in the second orbit?**

**Ans.** Since  $L = \frac{nh}{2\pi}$  where  $n = 2$

$$L = \frac{2h}{2\pi}$$

$$\Rightarrow L = \frac{h}{\pi}$$

**2 Mark Questions**

**1. Define Bohr's radius?**

**Ans.** The radius of the first orbit of hydrogen atom is called Bohr's radius.

It is equal to  $5.29 \times 10^{-11} m = 0.53 \text{ \AA}$ .

---

**2. State the limitations of Bohr's atomic model?**

**Ans.** (1) It does not give any indication regarding the arrangement and distribution of electrons in an atom.

(2) It could not account for the wave nature of electrons.



**3. Suppose you are given a chance to repeat the alpha-particle scattering experiment using a thin sheet of solid hydrogen in place of the gold foil. (Hydrogen is a solid at temperatures below 14 K.) What results do you expect?**

**Ans.** In the alpha-particle scattering experiment, if a thin sheet of solid hydrogen is used in place of a gold foil, then the scattering angle would not be large enough. This is because the mass of hydrogen ( $1.67 \times 10^{-27} \text{ kg}$ ) is less than the mass of incident  $\alpha$ -particles ( $6.64 \times 10^{-27} \text{ kg}$ ). Thus, the mass of the scattering particle is more than the target nucleus (hydrogen). As a result, the  $\alpha$ -particles would not bounce back if solid hydrogen is used in the  $\alpha$ -particle scattering experiment.

---

**4. The ground state energy of hydrogen atom is -13.6 eV. What are the kinetic and potential energies of the electron in this state?**

**Ans.** Ground state energy of hydrogen atom,  $E = -13.6 \text{ eV}$

This is the total energy of a hydrogen atom. Kinetic energy is equal to the negative of the total energy.

Kinetic energy =  $-E = -(-13.6) = 13.6 \text{ eV}$

Potential energy is equal to the negative of two times of kinetic energy.

Potential energy =  $-2 \times (13.6) = -27.2 \text{ eV}$

**5. If Bohr's quantisation postulate (angular momentum =  $nh/2\pi$ ) is a basic law of nature, it should be equally valid for the case of planetary motion also. Why then do we never speak of quantisation of orbits of planets around the sun?**

**Ans.** We never speak of quantization of orbits of planets around the Sun because the angular momentum associated with planetary motion is largely relative to the value of Planck's constant ( $h$ ). The angular momentum of the Earth in its orbit is of the order of  $1070h$ . This leads to a very high value of quantum levels  $n$  of the order of 1070. For large values of  $n$ , successive energies and angular momenta are relatively very small. Hence, the quantum levels for planetary motion are considered continuous.



### 3 Mark Questions

1. The half life period of a radioactive substance is 30 days. What is the time for  $\frac{3}{4}$ th of its original mass to disintegrate?

$$\text{Ans. } \frac{N}{N_0} = \left(\frac{1}{2}\right)^{\frac{t}{T}}$$

$$\text{Here } N = N_0 - \frac{3}{4}N_0$$

$$N = \frac{1}{4}N_0$$

$$\Rightarrow \frac{1}{4} = \left(\frac{1}{2}\right)^{\frac{t}{30}}$$

$$\text{Or } \left(\frac{1}{2}\right)^2 = \left(\frac{1}{2}\right)^{\frac{t}{30}}$$

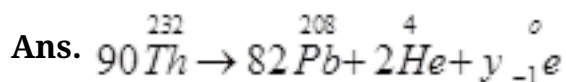
$$\frac{t}{30} = 2$$

Or

$$t = 60 \text{ days}$$

---

2. How many  $\alpha$  and  $\beta$ -particles are emitted when  ${}_{90}^{232}\text{Th}$  changes to  ${}_{82}^{208}\text{Pb}$



According to law of conservation of atomic number and mass number

$$90 = 82 + 2x - y$$

$$2x - y = 8 \text{ ----- (1)}$$

$$232 = 208 + 4x$$

$$\Rightarrow x = 6 \text{ ----- (2)}$$

From (1) & (2)

$$2(6) - y = 8$$

$$12 - 8 = y$$

Or

$$y = 4$$

---

3. Binding energies of  ${}^{16}_8\text{O}$  and  ${}^{35}_{17}\text{Cl}$  are 127.35 MeV and 289.3 MeV respectively.

**Which of the two nuclei are more stable?**

**Ans.** Stability of a nucleus is proportional to binding energy per nucleon

B.E / nucleon of

$${}^{16}_8\text{O} = \frac{127.35}{8} = 15.82 \text{ MeV / nucleon}$$

B.E / nucleon of

$${}^{35}_{17}\text{Cl} = \frac{289.3}{17} = 17.02 \text{ MeV / nucleon}$$

$\therefore {}^{35}_{17}\text{Cl}$  is more stable than  ${}^{16}_8\text{O}$

**4. What is the shortest wavelength present in the Paschen series of spectral lines?**

**Ans.**Rydberg's formula is given as:

$$\frac{hc}{\lambda} = 21.76 \times 10^{-19} \left[ \frac{1}{n_1^2} - \frac{1}{n_2^2} \right]$$

Where,

$$h = \text{Planck's constant} = 6.6 \times 10^{-34} \text{ Js}$$

$$c = \text{Speed of light} = 3 \times 10^8 \text{ m/s}$$

( $n_1$  and  $n_2$  are integers)

The shortest wavelength present in the Paschen series of the spectral lines is given for values  $n_1 = 3$  and  $n_2 = \infty$ .

$$\frac{hc}{\lambda} = 21.76 \times 10^{-19} \left[ \frac{1}{(3)^2} - \frac{1}{(\infty)^2} \right]$$

$$\lambda = \frac{6.6 \times 10^{-34} \times 3 \times 10^8 \times 9}{21.76 \times 10^{-19}}$$

$$= 8.189 \times 10^7 \text{ m}$$

$$= 818.9 \text{ nm}$$

---

**5. A difference of 2.3 eV separates two energy levels in an atom. What is the frequency of radiation emitted when the atom makes a transition from the upper level to the lower level?**

**Ans.**Separation of two energy levels in an atom,

$$E = 2.3 \text{ eV}$$

$$= 2.3 \times 1.6 \times 10^{-19}$$



$$= 3.68 \times 10^{-19} \text{ J}$$

Let  $\nu$  be the frequency of radiation emitted when the atom transits from the upper level to the lower level.

We have the relation for energy as:

$$E = h\nu$$

Where,

$$h = \text{Planck's constant} = 6.62 \times 10^{-34} \text{ Js}$$

$$\therefore \nu = \frac{E}{h}$$

$$= \frac{3.68 \times 10^{-19}}{6.62 \times 10^{-34}} = 5.55 \times 10^{14} \text{ Hz}$$

Hence, the frequency of the radiation is  $5.55 \times 10^{14}$  Hz.

---

**6. The radius of the innermost electron orbit of a hydrogen atom is  $5.3 \times 10^{-11} \text{ m}$ . What are the radii of the  $n = 2$  and  $n = 3$  orbits?**

**Ans.** The radius of the innermost orbit of a hydrogen atom,  $r_1 = 5.3 \times 10^{-11} \text{ m}$ .

Let  $r_2$  be the radius of the orbit at  $n = 2$ . It is related to the radius of the innermost orbit as:

$$r_2 = (n)^2 r_1$$

$$= 4 \times 5.3 \times 10^{-11} = 2.12 \times 10^{-10} \text{ m}$$

For  $n = 3$ , we can write the corresponding electron radius as:

$$r_3 = (n)^2 r_1$$

$$= 9 \times 5.3 \times 10^{-11} = 4.77 \times 10^{-10} \text{ m}$$

Hence, the radii of an electron for  $n = 2$  and  $n = 3$  orbits are  $2.12 \times 10^{-10} \text{ m}$  and  $4.77 \times 10^{-10} \text{ m}$  respectively.

**7. In accordance with the Bohr's model, find the quantum number that characterises the earth's revolution around the sun in an orbit of radius  $1.5 \times 10^{11} \text{ m}$  with orbital speed  $3 \times 10^4 \text{ m/s}$ . (Mass of earth =  $6.0 \times 10^{24} \text{ kg}$ .)**

**Ans.** Radius of the orbit of the Earth around the Sun,  $r = 1.5 \times 10^{11} \text{ m}$

Orbital speed of the Earth,  $v = 3 \times 10^4 \text{ m/s}$

Mass of the Earth,  $m = 6.0 \times 10^{24} \text{ kg}$

According to Bohr's model, angular momentum is quantized and given as:

$$mvr = \frac{nh}{2\pi}$$

Where,

$h$  = Planck's constant =  $6.62 \times 10^{-34} \text{ Js}$

$n$  = Quantum number

$$\begin{aligned} \therefore n &= \frac{mvr 2\pi}{h} \\ &= \frac{2\pi \times 6 \times 10^{24} \times 3 \times 10^4 \times 1.5 \times 10^{11}}{6.62 \times 10^{-34}} \\ &= 25.61 \times 10^{73} = 2.6 \times 10^{74} \end{aligned}$$

Hence, the quanta number that characterizes the Earth's revolution is  $2.6 \times 10^{74}$ .

**8. The total energy of an electron in the first excited state of the hydrogen atom is about -3.4 eV.**

**(a) What is the kinetic energy of the electron in this state?**

**(b) What is the potential energy of the electron in this state?**

**(c) Which of the answers above would change if the choice of the zero of potential energy is changed?**

**Ans.(a)** Total energy of the electron,  $E = -3.4 \text{ eV}$

Kinetic energy of the electron is equal to the negative of the total energy.

$$\Rightarrow K = -E$$

$$= -(-3.4) = +3.4 \text{ eV}$$

Hence, the kinetic energy of the electron in the given state is +3.4 eV.

**(b)** Potential energy ( $U$ ) of the electron is equal to the negative of twice of its kinetic energy.

$$\Rightarrow U = -2K$$

$$= -2 \times 3.4 = -6.8 \text{ eV}$$

Hence, the potential energy of the electron in the given state is -6.8 eV.

**(c)** The potential energy of a system depends on the reference point taken. Here, the potential energy of the reference point is taken as zero. If the reference point is changed, then the value of the potential energy of the system also changes. Since total energy is the sum of kinetic and potential energies, total energy of the system will also change.



### 5 Mark Questions

1. THE total energy of and electron in the first excited state of hydrogen atom is -3.4 eV.

Calculate

(1) K.E. of the electron in this state.

(2) P.E. of the electron in this state and

(3) Which of the answer would change if zero of PE is changed? Justify your answer?

Ans. (i) K.E = -E = 3.4eV

(ii) P.E = 02 × K.E

P.E = 02 × 3.4

(iii) If the zero of the P.E is changed, K.E remains unchanged but the P.E will change, hence total energy will change.

2. Prove that the speed of election in the ground sate of hydrogen atom is equal to the speed of electron in the first excited state of hydrogen like Li<sup>++</sup> atom.

Ans. 
$$v_n = \frac{2\pi Ke^2}{nh}$$

For ground state of hydrogen atom x = 1 
$$v_1 = \frac{2\pi Ke^2}{h}$$

From hydrogen like atom 
$$(v_n)_\mu = \frac{Z \times 2\pi Ke^2}{nh} \text{-----(1)}$$

For Li<sup>++</sup> atom z = 3 n = 2

$$\Rightarrow (v_n)_{Li^{++}} = \frac{2 \times 2\pi K e^2}{2h}$$

$$(v_n)_{Li^{++}} = \frac{2\pi K e^2}{h} \text{-----(2)}$$

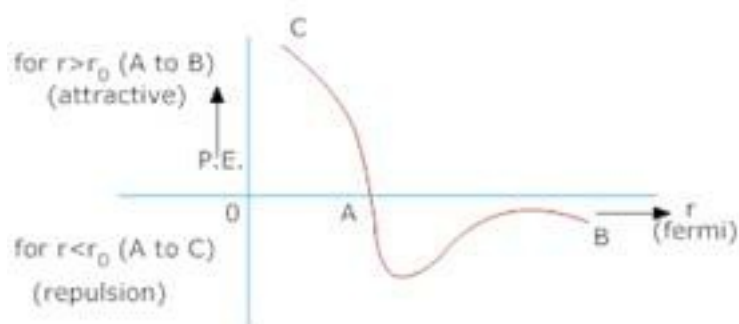
Hence from (1) and (2)

$$(v_n)_H = (v_n)_{Li^{++}}$$

**3. Draw a graph showing variation of potential energy of a pair of nucleon as a function of their separation indicate the region in which the nuclear force is (a) Attractive (b) Repulsive. Also write two characteristics features which distinguish it from the coulomb's force.**

**Ans.**(i) Nuclear forces are charge independent.

(ii) They are non – central forces.



**4. Choose the correct alternative from the clues given at the end of the each statement:**

**(a) The size of the atom in Thomson's model is ..... the atomic size in Rutherford's model. (much greater than/no different from/much less than.)**

**(b) In the ground state of ..... electrons are in stable equilibrium, while in .....**

electrons always experience a net force.

(Thomson's model/ Rutherford's model.)

(c) A *classical* atom based on ..... is doomed to collapse.

(Thomson's model/ Rutherford's model.)

(d) An atom has a nearly continuous mass distribution in a ..... but has a highly non-uniform mass distribution in .....

(Thomson's model/ Rutherford's model.)

(e) The positively charged part of the atom possesses most of the mass in .....

(Rutherford's model/both the models.)

**Ans.(a)** The sizes of the atoms taken in Thomson's model and Rutherford's model have the same order of magnitude.

**(b)** In the ground state of Thomson's model, the electrons are in stable equilibrium. However, in Rutherford's model, the electrons always experience a net force.

**(c)** A *classical* atom based on Rutherford's model is doomed to collapse.

**(d)** An atom has a nearly continuous mass distribution in Thomson's model, but has a highly non-uniform mass distribution in Rutherford's model.

**(e)** The positively charged part of the atom possesses most of the mass in both the models.

---

**5. A hydrogen atom initially in the ground level absorbs a photon, which excites it to the  $n = 4$  level. Determine the wavelength and frequency of the photon.**

**Ans.** For ground level,  $n_1 = 1$

Let  $E_1$  be the energy of this level. It is known that  $E_1$  is related with  $n_1$  as:

$$E_1 = \frac{-13.6}{n_1^2}$$



$$= \frac{-13.6}{1^2} = -13.6 \text{ eV}$$

The atom is excited to a higher level,  $n_2 = 4$ .

Let  $E_2$  be the energy of this level.

$$\begin{aligned}\therefore E_2 &= \frac{-13.6}{n_2^2} \text{ eV} \\ &= \frac{-13.6}{4^2} = -13.6 \text{ eV}\end{aligned}$$

The amount of energy absorbed by the photon is given as:

$$\begin{aligned}E &= E_2 - E_1 \\ &= \frac{-13.6}{16} - \left( -\frac{13.6}{1} \right) \\ &= \frac{13.6 \times 15}{16} \text{ eV} \\ &= \frac{13.6 \times 15}{16} \times 1.6 \times 10^{-19} = 2.04 \times 10^{-18} \text{ J}\end{aligned}$$

For a photon of wavelength  $\lambda$ , the expression of energy is written as:

$$E = \frac{hc}{\lambda}$$

Where,

$h$  = Planck's constant =  $6.6 \times 10^{-34} \text{ Js}$

$c$  = Speed of light =  $3 \times 10^8 \text{ m/s}$

$$\therefore \lambda = \frac{hc}{E}$$

$$= \frac{6.6 \times 10^{-34} \times 3 \times 10^8}{2.04 \times 10^{-18}}$$

$$= 9.7 \times 10^{-8} \text{ m} = 97 \text{ nm}$$

And, frequency of a photon is given by the relation,

$$v = \frac{c}{\lambda}$$

$$= \frac{3 \times 10^8}{9.7 \times 10^{-8}} \approx 3.1 \times 10^{15} \text{ Hz}$$

Hence, the wavelength of the photon is 97 nm while the frequency is  $3.1 \times 10^{15} \text{ Hz}$ .

**6. (a) Using the Bohr's model calculate the speed of the electron in a hydrogen atom in the  $n = 1, 2,$  and  $3$  levels. (b) Calculate the orbital period in each of these levels.**

**Ans. (a)** Let  $v_1$  be the orbital speed of the electron in a hydrogen atom in the ground state level,  $n_1 = 1$ . For charge ( $e$ ) of an electron,  $v_1$  is given by the relation,

$$v_1 = \frac{e^2}{n_1 4\pi \epsilon_0 \left( \frac{h}{2\pi} \right)} = \frac{e^2}{2 \epsilon_0 h}$$

Where,

$$e = 1.6 \times 10^{-19} \text{ C}$$

$$\epsilon_0 = \text{Permittivity of free space} = 8.85 \times 10^{-12} \text{ N}^{-1} \text{ C}^2 \text{ m}^{-2}$$

$$h = \text{Planck's constant} = 6.62 \times 10^{-34} \text{ Js}$$

$$\therefore v_1 = \frac{(1.6 \times 10^{-19})^2}{2 \times 8.85 \times 10^{-12} \times 6.62 \times 10^{-34}}$$

$$= 0.0218 \times 10^8 = 2.18 \times 10^6 \text{ m/s}$$

For level  $n_2 = 2$ , we can write the relation for the corresponding orbital speed as:

$$\begin{aligned}v_1 &= \frac{e^2}{n_2 2 \epsilon_0 h} \\&= \frac{(1.6 \times 10^{-19})^2}{2 \times 2 \times 8.85 \times 10^{-22} \therefore 6.62 \times 10^{-34}} \text{ s} \\&= 1.09 \times 10^6 \text{ m/s}\end{aligned}$$

And, for  $n_3 = 3$ , we can write the relation for the corresponding orbital speed as:

$$\begin{aligned}v_3 &= \frac{e^2}{n_2 2 \epsilon_0 h} \\&= \frac{(1.6 \times 10^{-19})^2}{3 \times 2 \times 8.85 \times 10^{-12} \times 6.62 \times 10^{-34}} \\&= 7.27 \times 10^6 \text{ m/s}\end{aligned}$$

Hence, the speed of the electron in a hydrogen atom in  $n = 1, n=2$ , and  $n=3$  is  $2.18 \times 10^6$  m/s,  $1.09 \times 10^6$  m/s,  $7.27 \times 10^5$  m/s respectively.

**(b)** Let  $T_1$  be the orbital period of the electron when it is in level  $n_1 = 1$ .

Orbital period is related to orbital speed as:

$$T_1 = \frac{2\pi r_1}{v_1}$$

Where,

$r_1$  = Radius of the orbit

$$= \frac{n_1^2 h^2 \epsilon_0}{\pi m e^2}$$

$h$  = Planck's constant =  $6.62 \times 10^{-34} \text{ Js}$

$e$  = Charge on an electron =  $1.6 \times 10^{-19} \text{ C}$

$\epsilon_0$  = Permittivity of free space =  $8.85 \times 10^{-12} \text{ N}^{-1} \text{ C}^2 \text{ m}^{-2}$

$m$  = Mass of an electron =  $9.1 \times 10^{-31} \text{ kg}$

$$\begin{aligned}\therefore T_1 &= \frac{2\pi r_1}{v_1} \\ &= \frac{2\pi \times (1)^2 \times (6.62 \times 10^{-34})^2 \times 8.85 \times 10^{-12}}{2.18 \times 10^6 \times \pi \times 9.1 \times 10^{-31} \times (1.6 \times 10^{-19})^2} \\ &= 15.27 \times 10^{-17} = 1.527 \times 10^{-16}\end{aligned}$$

For level  $n_2 = 2$ , we can write the period as:

$$T_2 = \frac{2\pi r_2}{v_2}$$

Where,

$r_2$  = Radius of the electron in  $n_2 = 2$

$$\begin{aligned}&= \frac{(n_2)^2 h^2 \epsilon_0}{\pi m e^2} \\ \therefore T_2 &= \frac{2\pi \times (2)^2}{v_2} \\ &= \frac{2\pi \times (2)^2 \times (6.62 \times 10^{-34})^2 \times 8.85 \times 10^{-12}}{1.09 \times 10^6 \times \pi \times 9.1 \times 10^{-31} \times (1.6 \times 10^{-19})^2} \\ &= 1.22 \times 10^{-15}\end{aligned}$$

And, for level  $n_3 = 3$ , we can write the period as:

$$T_3 = \frac{2\pi r_3}{v_3}$$

Where,

$$r_3 = \text{Radius of the electron in } n_3 = 3 \frac{(n_3)^2 h^2 \epsilon_0}{\pi m e^2}$$

$$\therefore T_3 = \frac{2\pi r_3}{v_3}$$

$$\begin{aligned} & \frac{(n_3)^2 h^2 \epsilon_0}{\pi m e^2} \\ &= \frac{2\pi \times (3)^2 \times (6.62 \times 10^{-34})^2 \times 8.85 \times 10^{-12}}{7.27 \times 10^5 \times \pi \times 9.1 \times 10^{-31} \times (1.6 \times 10^{-19})^2} \\ &= 4.12 \times 10^{-15} \end{aligned}$$

$$\therefore T_3 = \frac{2\pi r_3}{v_3}$$

Hence, the orbital period in each of these levels is  $1.52 \times 10^{-15} \text{ s}$ ,  $1.22 \times 10^{-15} \text{ s}$ , and  $4.12 \times 10^{-15} \text{ s}$  respectively.

**Q9. A 12.5 eV electron beam is used to bombard gaseous hydrogen at room temperature. What series of wavelengths will be emitted?**

**Ans.** It is given that the energy of the electron beam used to bombard gaseous hydrogen at room temperature is 12.5 eV. Also, the energy of the gaseous hydrogen in its ground state at room temperature is - 13.6 eV.

When gaseous hydrogen is bombarded with an electron beam, the energy of the gaseous



hydrogen becomes  $-13.6 + 12.5$  eV i.e.,  $-1.1$  eV.

Orbital energy is related to orbit level ( $n$ ) as:

$$E = \frac{-13.6}{(n)^2} eV$$

$$\text{For } n = 3, E = \frac{-13.6}{9} = -1.5 eV$$

This energy is approximately equal to the energy of gaseous hydrogen. It can be concluded that the electron has jumped from  $n = 1$  to  $n = 3$  level.

During its de-excitation, the electrons can jump from  $n = 3$  to  $n = 1$  directly, which forms a line of the Lyman series of the hydrogen spectrum.

We have the relation for wave number for Lyman series as:

$$\frac{1}{\lambda} = R_y \left( \frac{1}{l^2} - \frac{1}{n^2} \right)$$

Where,

$$R_y = \text{Rydberg constant} = 1.097 \times 10^7 m^{-1}$$

$\lambda$  = Wavelength of radiation emitted by the transition of the electron

For  $n = 3$ , we can obtain  $\lambda$  as:

$$\begin{aligned} \frac{1}{\lambda} &= 1.097 \times 10^7 \left( \frac{1}{l^2} - \frac{1}{3^2} \right) \\ &= 1.097 \times 10^7 \left( 1 - \frac{1}{9} \right) = 1.097 \times 10^7 \times \frac{8}{9} \end{aligned}$$

$$\lambda = \frac{9}{8 \times 1.097 \times 10^7} = 102.55 nm$$

If the electron jumps from  $n = 2$  to  $n = 1$ , then the wavelength of the radiation is given as:



$$\frac{1}{\lambda} = 1.097 \times 10^7 \left( \frac{1}{1^2} - \frac{1}{2^2} \right)$$

$$= 1.097 \times 10^7 \left( 1 - \frac{1}{4} \right) = 1.097 \times 10^7 \times \frac{3}{4}$$

$$\lambda = \frac{4}{1.097 \times 10^7 \times 3} = 121.54 \text{ nm}$$

If the transition takes place from  $n = 3$  to  $n = 2$ , then the wavelength of the radiation is given as:

$$\frac{1}{\lambda} = 1.097 \times 10^7 \left( \frac{1}{2^2} - \frac{1}{3^2} \right)$$

$$= 1.097 \times 10^7 \left( \frac{1}{4} - \frac{1}{9} \right) = 1.097 \times 10^7 \times \frac{5}{36}$$

$$\lambda = \frac{36}{5 \times 1.097 \times 10^7} = 656.33 \text{ nm}$$

This radiation corresponds to the Balmer series of the hydrogen spectrum. Hence, in Lyman series, two wavelengths i.e., 102.5 nm and 121.5 nm are emitted. And in the Balmer series, one wavelength i.e., 656.33 nm is emitted.

**10. Answer the following questions, which help you understand the difference between Thomson's model and Rutherford's model better.**

- (a) Is the average angle of deflection of  $\alpha$ -particles by a thin gold foil predicted by Thomson's model much less, about the same, or much greater than that predicted by Rutherford's model?
- (b) Is the probability of backward scattering (i.e., scattering of  $\alpha$ -particles at angles greater than  $90^\circ$ ) predicted by Thomson's model much less, about the same, or much greater than that predicted by Rutherford's model?
- (c) Keeping other factors fixed, it is found experimentally that for small thickness  $t$ , the

**number of  $\alpha$ -particles scattered at moderate angles is proportional to  $t$ . What clue does this linear dependence on  $t$  provide?**

**(d) In which model is it completely wrong to ignore multiple scattering for the calculation of average angle of scattering of  $\alpha$ -particles by a thin foil?**

**Ans.(a)** about the same

The average angle of deflection of  $\alpha$ -particles by a thin gold foil predicted by Thomson's model is about the same size as predicted by Rutherford's model. This is because the average angle was taken in both models.

**(b)** much less

The probability of scattering of  $\alpha$ -particles at angles greater than  $90^\circ$  predicted by Thomson's model is much less than that predicted by Rutherford's model.

**(c)** Scattering is mainly due to single collisions. The chances of a single collision increases linearly with the number of target atoms. Since the number of target atoms increase with an increase in thickness, the collision probability depends linearly on the thickness of the target.

**(d)** Thomson's model

It is wrong to ignore multiple scattering in Thomson's model for the calculation of average angle of scattering of  $\alpha$ -particles by a thin foil. This is because a single collision causes very little deflection in this model. Hence, the observed average scattering angle can be explained only by considering multiple scattering.

---

**11. The gravitational attraction between electron and proton in a hydrogen atom is weaker than the coulomb attraction by a factor of about  $10^{-14}$ . An alternative way of looking at this fact is to estimate the radius of the first Bohr orbit of a hydrogen atom if the electron and proton were bound by gravitational attraction. You will find the answer interesting.**

**Ans.**Radius of the first Bohr orbit is given by the relation,



$$r_1 = \frac{4\pi\epsilon_0 \left(\frac{h}{2\pi}\right)^2}{m_e e^2} \dots\dots\dots(1)$$

Where,

$\epsilon_0$  = Permittivity of free space

$h$  = Planck's constant =  $6.63 \times 10^{-34}$  Js

$m_e$  = Mass of an electron =  $9.1 \times 10^{-31}$  kg

$e$  = Charge of an electron =  $1.9 \times 10^{-19}$  C

$m_p$  = Mass of a proton =  $1.67 \times 10^{-27}$  kg

$r$  = Distance between the electron and the proton

Coulomb attraction between an electron and a proton is given as:

$$F_G = \frac{e^2}{4\pi\epsilon_0 r^2} \dots\dots\dots(2)$$

Gravitational force of attraction between an electron and a proton is given as:

$$F_G = \frac{Gm_p m_e}{r_2} \dots\dots\dots(3)$$

Where,

$G$  = Gravitational constant =  $6.67 \times 10^{-11}$  N m<sup>2</sup> / kg<sup>2</sup>

If the electrostatic (Coulomb) force and the gravitational force between an electron and a proton are equal, then we can write:

$\therefore F_G = F_C$

$$\frac{Gm_p m_e}{r_2} = \frac{e^2}{4\pi\epsilon_0 r^2}$$

$$\therefore \frac{e^2}{4\pi\epsilon_0} = Gm_p m_e \dots \dots \dots (4)$$

Putting the value of equation (4) in equation (1), we get:

$$r_1 = \frac{\left(\frac{h}{2\pi}\right)^2}{Gm_p m_e^2}$$

$$= \frac{\left(\frac{6.63 \times 10^{-34}}{2 \times 3.14}\right)^2}{6.67 \times 10^{-11} \times 1.67 \times 10^{-27} \times (9.1 \times 10^{-31})^2} \approx 1.21 \times 10^{29} m$$

It is known that the universe is 156 billion light years wide or  $1.5 \times 10^{27} m$  wide. Hence, we can conclude that the radius of the first Bohr orbit is much greater than the estimated size of the whole universe.

**12. Obtain an expression for the frequency of radiation emitted when a hydrogen atom de-excites from level  $n$  to level  $(n-1)$ . For large  $n$ , show that this frequency equals the classical frequency of revolution of the electron in the orbit.**

**Ans.** It is given that a hydrogen atom de-excites from an upper level ( $n$ ) to a lower level ( $n - 1$ ). We have the relation for energy ( $E_1$ ) of radiation at level  $n$  as:

$$E_1 = h\nu_1 = \frac{h m e^4}{(4\pi)^3 \epsilon_0^2 \left(\frac{h}{2\pi}\right)^3} \times \left(\frac{1}{n^2}\right) \dots \dots (i)$$

Where,

$\nu_1$  = Frequency of radiation at level  $n$

$h$  = plank's constant

$m$  = mass of hydrogen atom

$e$  = charge on an electron

$\epsilon_0$  = Permittivity of free space

Now, the relation for energy ( $E_2$ ) of radiation at level ( $n - 1$ ) is given as:

$$E_2 = h\nu_2 = \frac{hme^4}{(4\pi)^3 \epsilon_0^2 \left(\frac{h}{2\pi}\right)^3} \times \frac{1}{(n-1)^2} \dots\dots (ii)$$

Where,

$\nu_2$  = Frequency of radiation at level ( $n-1$ )

Energy ( $E$ ) released as a result of de-excitation:

$$E = E_2 - E_1$$

$$h\nu = E_2 - E_1 \dots (iii)$$

Where,

$\nu$  = Frequency of radiation emitted

Putting values from equations (i) and (ii) in equation (iii), we get:

$$\begin{aligned} \nu &= \frac{me^4}{(4\pi)^3 \epsilon_0^2 \left(\frac{h}{2\pi}\right)^3} \left[ \frac{1}{(n-1)^2} - \frac{1}{n^2} \right] \\ &= \frac{me^4 (2n-1)}{(4\pi)^3 \epsilon_0^2 \left(\frac{h}{2\pi}\right)^3 n^2 (n-1)^2} \end{aligned}$$

For large  $n$ , we can write  $(2n-1) \approx 2n$  and  $(n-1) \approx n$

$$\therefore v = \frac{me^4}{32\pi\epsilon_0^2 \left(\frac{h}{2\pi}\right)^3 n^3} \dots\dots\dots(iv)$$

Classical relation of frequency of revolution of an electron is given as:

$$v_c = \frac{v}{2\pi r} \dots\dots(v)$$

Where,

Velocity of the electron in the  $n$ th orbit is given as:

$$v = \frac{e^2}{4\pi\epsilon_0 \left(\frac{h}{2\pi}\right)n} \dots\dots(vi)$$

And, radius of the  $n$ th orbit is given as:

$$r = \frac{4\pi\epsilon_0 \left(\frac{h}{2\pi}\right)^2}{me^2} n^2 \dots\dots(vii)$$

Putting the values of equations (vi) and (vii) in equation (v), we get:

$$v_c = \frac{me^4}{32\pi^3 \epsilon_0^2 \left(\frac{h}{2\pi}\right)^3 n^3} \dots\dots(viii)$$

Hence, the frequency of radiation emitted by the hydrogen atom is equal to its classical orbital frequency.

**13. classically, an electron can be in any orbit around the nucleus of an atom. Then what determines the typical atomic size? Why is an atom not, say, thousand times bigger**

than its typical size? The question had greatly puzzled Bohr before he arrived at his famous model of the atom that you have learnt in the text. To simulate what he might well have done before his discovery, let us play as follows with the basic constants of nature and see if we can get a quantity with the dimensions of length that is roughly equal to the known size of an atom ( $\sim 10^{-10} \text{ m}$ ).

(a) Construct a quantity with the dimensions of length from the fundamental constants  $e$ ,  $m_e$ , and  $c$ . Determine its numerical value.

(b) You will find that the length obtained in (a) is many orders of magnitude smaller than the atomic dimensions. Further, it involves  $c$ . But energies of atoms are mostly in non-relativistic domain where  $c$  is not expected to play any role. This is what may have suggested Bohr to discard  $c$  and look for 'something else' to get the right atomic size. Now, the Planck's constant  $h$  had already made its appearance elsewhere. Bohr's great insight lay in recognising that  $h$ ,  $m_e$ , and  $e$  will yield the right atomic size. Construct a quantity with the dimension of length from  $h$ ,  $m_e$ , and  $e$  and confirm that its numerical value has indeed the correct order of magnitude.

Ans.(a) Charge on an electron,  $e = 1.6 \times 10^{-19} \text{ C}$

Mass of an electron,  $m_e = 9.1 \times 10^{-31} \text{ kg}$

Speed of light,  $c = 3 \times 10^8 \text{ m/s}$

Let us take a quantity involving the given quantities as  $\left( \frac{e^2}{4\pi\epsilon_0 m_e c^2} \right)$

Where,

$\epsilon_0$  = Permittivity of free space

And,  $\frac{1}{4\pi\epsilon_0} = 9 \times 10^9 \text{ Nm}^2\text{C}^{-2}$

The numerical value of the taken quantity will be:



$$\frac{1}{4\pi\epsilon_0} \times \frac{e^2}{m_e c^2}$$

$$= 9 \times 10^9 \times \frac{(1.6 \times 10^{-19})^2}{9.1 \times 10^{-31} \times (3 \times 10^8)^2}$$

$$= 2.81 \times 10^{-15} m$$

Hence, the numerical value of the taken quantity is much smaller than the typical size of an atom.

**(b)** Charge on an electron  $e = 1.6 \times 10^{-19} C$

Mass of an electron,  $m_e = 9.1 \times 10^{-31} kg$

Planck's constant,  $h = 6.63 \times 10^{-34} Js$

Let us take a quantity involving the given quantities as  $\left( \frac{e^2}{4\pi\epsilon_0 m_e c^2} \right)$ .

Where,

$\epsilon_0$  = Permittivity of free space

And,  $\frac{1}{4\pi\epsilon_0} = 9 \times 10^9 Nm^2C^{-2}$

The numerical value of the taken quantity will be:

$$\frac{1}{4\pi\epsilon_0} \times \frac{(1.6 \times 10^{-19})^2}{9.1 \times 10^{-31} \times (3 \times 10^8)^2}$$

$$= 2.81 \times 10^{-15} m$$

Hence, the value of the quantity taken is of the order of the atomic size.

**14. Obtain the first Bohr's radius and the ground state energy of a *muonic hydrogen atom* [i.e., an atom in which a negatively charged muon ( $\mu^-$ ) of mass about  $207m_e$  orbits around a proton].**

**Ans.** Mass of a negatively charged muon,  $m_{\mu^-} = 207m_e$

According to Bohr's model,

$$\text{Bohr radius, } r_e \propto \left( \frac{1}{m_c} \right)$$

And, energy of a ground state *electronic hydrogen atom*,  $E_e \propto m_c$ .

We have the value of the first Bohr orbit,  $r_e = 0.53 \text{ \AA} = 0.53 \times 10^{-10} \text{ m}$

Let  $r_{\mu}$  be the radius of *muonic hydrogen atom*.

At equilibrium, we can write the relation as:

$$m_{\mu} r_{\mu} = m_e r_e$$

$$207m_e \times r_{\mu} = m_e r_e$$

$$\therefore r_{\mu} = \frac{0.53 \times 10^{-10}}{207} = 2.56 \times 10^{-13} \text{ m}$$

Hence, the value of the first Bohr radius of a *muonic hydrogen atom* is

$2.56 \times 10^{-13} \text{ m}$ . We have,

$$E_e = -13.6 \text{ eV}$$

Take the ratio of these energies as:

$$\frac{E_e}{E_{\mu}} = \frac{m_e}{m_{\mu}} = \frac{m_e}{207m_e}$$

$$E_{\mu} = 207E_e$$

$$= 207 \times (-13.6) = -2.81 \text{ keV}$$

Hence, the ground state energy of a muonic hydrogen atom is - 2.81 keV.